

Math 151

Nov. 19, 2019

Test #3 A

Name _____

(please print)

Show Your Work!

Good Luck!

1. $x^3 + x^2y^3 + 6\sin(3y) = y^2 + 1$. (Show your work!)

(4) (a) Calculate y' at $(1, 0)$. $y' =$ _____

(3) (b) The equation of the tangent line to this curve at $(1, 0)$ is $L(x) =$ _____

(2) (c) Use the tangent line in part (b) to approximate y when $x=1.03$. $y \approx$ _____

(b) Use **log. differentiation**: $\frac{d}{dx}(5 + \sin(x))^x =$

(5) (circle your answer)

2. True or False (circle the correct answer)

(2) True False If $g(x)$ is differentiable and decreasing for $1 \leq x \leq 6$ then $g'(4) < 0$.

(2) True False If $f(3)$ is a local maximum for f , then $f'(3) = 0$.

(2) True False If $g'(2)$ is undefined then $g(2)$ is a local max or local min.

(2) True False If $\lim_{x \rightarrow 1} g(x) = \lim_{x \rightarrow 1} f(x) = 0$, and then $\lim_{x \rightarrow 1} \frac{f(x)}{g(x)} = 1$.

(2) True False If $f'(2) = 0$ and $f''(2) < 0$ then f has a local maximum at $x=2$.

3. The graph of $y = f'(x)$ is shown.

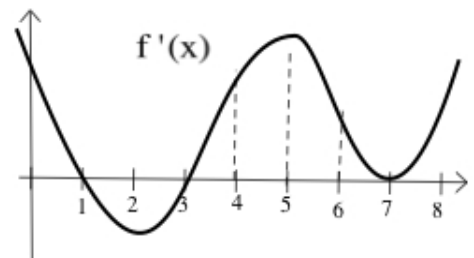
(2) (a) At $x=3$ f has a local MAX MIN NEITHER (circle one).

(2) (b) At $x=5$ f has a local MAX MIN NEITHER (circle one).

(2) (c) At $x=7$ f is INCREASING DECREASING NEITHER (circle one)

(2) (d) At $x=4$ f is concave UP DOWN NEITHER (circle one)

(2) (e) f has an Inflection Point at $x =$ _____

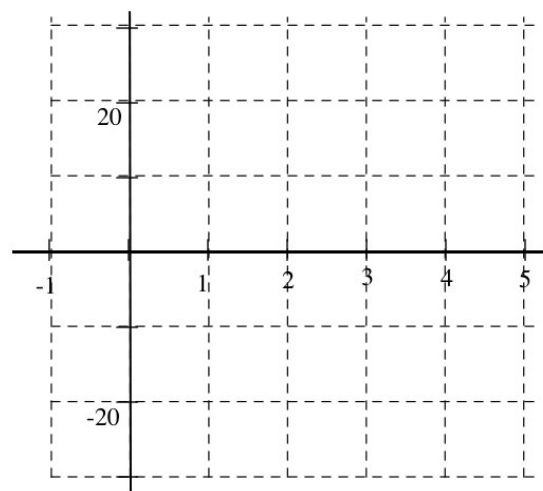


4. $f(x) = x^3 - 9x^2 + 24x + 3$ on the interval $-1 \leq x \leq 5$.

Use **CALCULUS** to answer these.

- (4) (a) f has critical numbers at $x =$ _____
 (2) (b) f has local maximum(s) at $x =$ _____
 (2) (c) The global minimum value of f is _____
 (2) at $x =$ _____
 (2) (d) at $x=2$ the graph of $f(x)$ is concave UP DOWN NEITHER
 (2) (e) f has Inflection Point(s) at $x =$ _____
 (4) (f) Sketch a **good** graph of f
 (4) (g) According to the Mean Value Theorem there is a value $x=c$
 between -1 and 5 so that $f'(c) =$ _____

(Show your **calculus** work. No work = no points.)



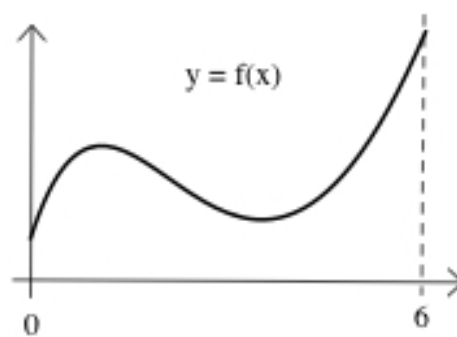
5. (a) The graph of $y = f(x)$ is shown for $0 \leq x \leq 6$.

Plot and label the location(s) of the c values

- (2) from the Mean Value Theorem.

- (b) According to the Mean Value Theorem, if the temperature increased 21 degrees from 1 PM to 8 PM then

- (2) _____ (fill in)



6. $f'(x) = (x)(x-2)^2(x-5)$ (circle the correct answer)

- (2) (a) At $x=1$ f is Increasing Decreasing Neither
 (2) (b) At $x=3$ f is Increasing Decreasing Neither
 (2) (c) $f(2)$ is LocalMax LocalMin Neither
 (2) (d) $f(5)$ is LocalMax LocalMin Neither

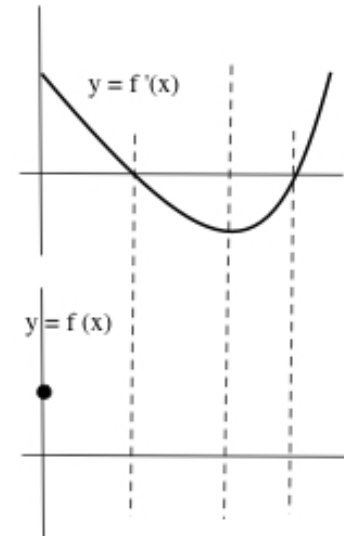
7. $f'(x) = 12x^3 + 8e^{2x} - 4\cos(x) + 5$ and $f(0) = 9$.

Then $f(x) =$ _____

(6)

8. The graph of $y = f'(x)$ is shown on the top graph and $f(0)$ is the dot on the bottom graph. On the bottom axis sketch a good graph of $y = f(x)$.

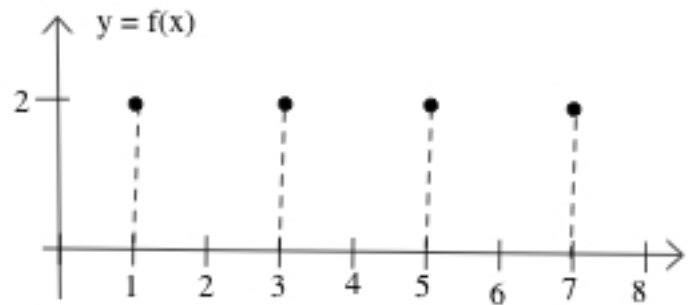
(4)



9. On the given axes sketch a continuous function $y = f(x)$ so that

$f(1) = f(3) = f(5) = f(7) = 2$ (those points are on the figure)

- (2) (a) $f'(1) = -1$ and $f''(1) > 0$
 (2) (b) $f'(3) = 0$ and $x=3$ is NOT a local max or min of f
 (2) (c) $f'(5) = -1$ and $x=5$ is an Inflection Point of f
 (2) (d) $f'(7)$ is undefined and f is decreasing at $x=7$



10. If the units of x are dollars and the units of y are miles then

the units of $\frac{d^2y}{dx^2} = y''$ are _____

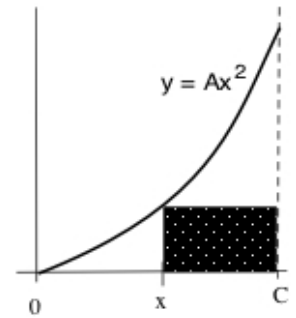
(2)

11. Do **TWO** of these max/min problems. (If you do all 3 I will only grade A and B. (6 points each)

(Show your work. Organize your work so I can understand it. No work = no points.)

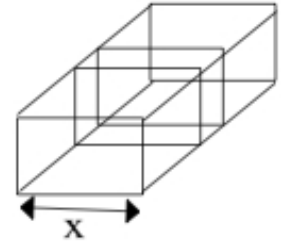
A. Find the value of x (in terms of A and C) that maximizes the shaded area.

$$x = \underline{\hspace{2cm}}$$



B. You have 150 square inches of tin to build a box (no top) that has two dividers (see figure) and is 2 times as long as it is wide (put x = width). What dimensions will maximize the volume? (integers or 2 decimal places)

$$x = \text{width} = \underline{\hspace{2cm}} \quad \text{length} = \underline{\hspace{2cm}} \quad \text{height} = \underline{\hspace{2cm}}$$

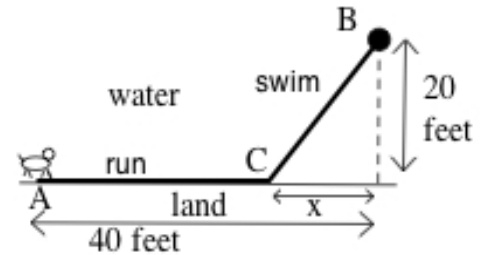


C. Your very smart dog starts at A (see figure) and wants to reach the ball at B as quickly as possible. The dog can run at 5 feet/second and can swim at 2 feet/second. The dog runs along the land from A to C and then swims from C to B. What value of x will minimize the total time to reach the ball?

$$x = \underline{\hspace{2cm}} \quad (2 \text{ decimal places})$$

A B C

A B C



BONUS (+2 if correct)

Name the two co-inventors of calculus: _____ and _____

The end!! (Total = 100 + 2 bonus.) Tests back tomorrow.