Show your work.

Name $\qquad$

1. $g(x)$ is a continuous function $\qquad$ $\rightarrow$
(a) $g(x)=0$ at least $\qquad$ times
(b) $g(x)=3$ at least $\qquad$ times

| x | 0 | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | ---: | ---: | ---: | ---: | ---: |
| $\mathrm{~g}(\mathrm{x})$ | 2 | 5 | -2 | 3 | 1 | -3 |

(c) $g(x)=-1$ at least $\qquad$ times
2. (a) Define $f^{\prime}(x)=$
(2) (the definition)
(2) (b) What does $\mathrm{f}^{\prime}$ ( x ) measure? (just give one)

$y=$ SLOPE of $f$
3. The graph of $\mathrm{y}=\mathrm{f}(\mathrm{x})$ is shown.

On the lower axes graph $\mathrm{y}=\{$ slope of $\mathrm{f}(\mathrm{x})\}$
(3)
4. $g(x)=\left\{\begin{array}{lll}x+K & \text { if } & x \leq 3 \\ x^{2}+2 & \text { if } & 3<x\end{array}\right\}$

What value of K will make $\mathrm{g}(\mathrm{x})$ continuous at $\mathrm{x}=3$ ? $\mathrm{K}=$ $\qquad$
(1)
5. (a) $f(x)=x^{2}+3 x+1$. Evaluate and simplify (no limit) $\frac{f(2+c)-f(2)}{c}=$ $\qquad$
(3)
6. What is the equation of the line tangent to the graph of

$$
f(x)=x^{3}-2 x+1 \quad \text { when } x=2 ?
$$

$$
y=
$$

$\qquad$
(4)
7. $f(x)=5 x^{2}-3 x+7$. At what value of x is $\mathrm{f} '(\mathrm{x})=2 ? \mathrm{x}=$ $\qquad$
(1)

$$
\mathrm{D}\left(3 x+\frac{2}{x}\right)=
$$

$\qquad$
(1)
8. If the units of $x$ are fish and the units of $f(x)$ are trees, then the units of $f$ ' $(x)$ are $\qquad$
(1)

Bonus ( +1 if correct) Name one project or field of mathematics that John von Neumann worked in. $\qquad$

